



JURONG SECONDARY SCHOOL 2022 GRADUATION EXAMINATION 2 SECONDARY 4 EXPRESS/ SECONDARY 5 NORMAL (ACADEMIC)

NAME	
CLASS	INDEX NUMBER
MATHEMATICS	4048/0

MATHEMATICS

PAPER 1

26 Aug 2022 2 hours

Candidates answer on the Question paper.

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number on all the work you hand in. Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

Answer all the questions.

If working is needed for any question it must be shown with the answer.

Omission of essential working will result in loss of marks.

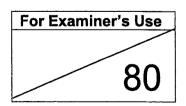
The use of an approved scientific calculator is expected, where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place. For π , use either your calculator value or 3.142, unless the question requires the answer in

terms of π .

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question. The total number of marks for this paper is 80.



This document consists of 23 printed pages, including this page.

4048/1/GE2/22

[Turn Overl

Mathematical Formulae

Compound interest

Total amount =
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone = πrl

Surface area of a sphere $=4\pi r^2$

Volume of a cone
$$=\frac{1}{3}\pi r^2 h$$

Volume of a sphere
$$=\frac{4}{3}\pi r^3$$

Area of triangle
$$ABC = \frac{1}{2}ab\sin C$$

Arc length = $r\theta$, where θ is in radians

Sector area
$$=\frac{1}{2}r^2\theta$$
, where θ is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Statistics

$$Mean = \frac{\sum fx}{\sum f}$$

Standard deviation =
$$\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

Answer	[1	[]
--------	----	----

The ratio of interior angle: exterior angle of a regular polygon is 5:1.

Calculate the number of sides that the polygon has.

Answer	sides	1	1

3 A photocopier can photocopy at a rate of 30 double-sided papers per minute.

Calculate

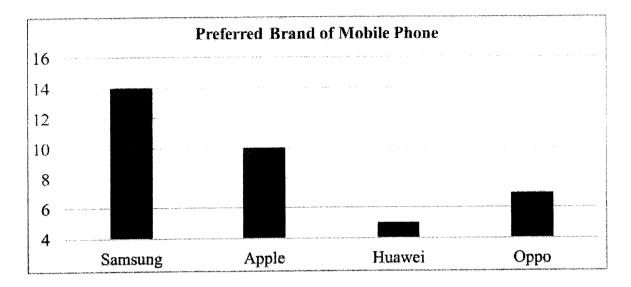
(a) in minutes, the time taken to print 600 pages on double-sided setting,

(b) the number of double-sided papers that can be photocopied in 1 hour.

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[Turn Over]

A survey was conducted to find out the preferred brand of mobile phone that secondary school students like.

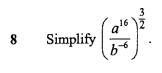


State one aspect of the graph that may be misleading and explain how this may lead to a misinterpretation of the graph.

•••••	********	***************************************	*********	
• • • • • • • • • • • • • • • • • • • •			•••••	
				[2]

Solve the inequality $-2+x \le 2-3x < 9+4x$.

6	Find a possible set of integer values $ax + by = 1$	s of a and b such that the lines $x+y=1$ and
	(a) do not intersect,	
		Answer $a = \dots$ $b = \dots [1]$
	(b) intersect at exactly one point.	
		Answer $a = \dots $ $b = \dots $ [1]
7	Factorise $4ax^2 - 4ay^2 + 2bx^2 - 2by^2$ co	
	-	
		Answer[2]



Answer			• • • • • • •		. 	[2]
--------	--	--	---------------	--	-----------	-----

Given that $25 \times 125^x = 5$, find the value of x.

10 Solve
$$\frac{5}{(2-x)^2} + \frac{1}{x-2} = 4$$
.

Answer	x	=														•	٠.						••	[3]	
--------	---	---	--	--	--	--	--	--	--	--	--	--	--	--	--	---	----	--	--	--	--	--	----	----	---	--

11 (a) Express $1+x^2-5x$ in the form of $(x+a)^2+b$.

(b) Write down the equation of line of symmetry of the graph of $y = 1 + x^2 - 5x$.

(c) Write down the coordinates of intersection between the line of symmetry and the graph of $y = 1 + x^2 - 5x$.

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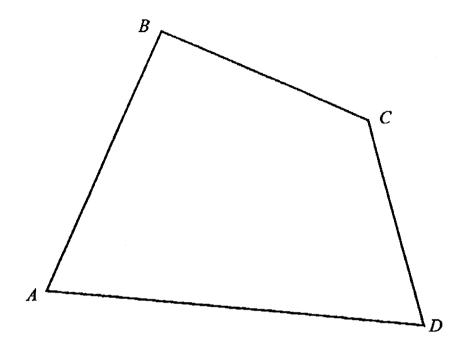
[Turn Over]

12	The area of triangle ABC is 7.5 cm ² . Two of the sides are of length 5 cm and 6 cm respectively. Find the length of the third side.
	<i>Answer</i> cm [3]
	Answer
13	The Ideal Gas Law
	PV = 8.3145nT
	relates pressure P (measured in Pascal), volume V (measured in metres ³), the number of moles of a gas n (measured in moles), and temperature T (measured in Kelvins).
	One mole of gas is found to exert a pressure of 101 325 Pascal at room temperature 293 Kelvins. Find the volume of the gas in cm ³ .
	Answercm ³ [2]

14	A m	ap of the United States of America has a scale of 1:8 000 000.								
	(a)	The length of the Mississippi River is 3766 km. Calculate the length, in centimetres, of Mississippi River on the map.								
	(b)	Answercm [1] The area of California on the map is 66.25 cm ² . Calculate the actual area, in square kilometres, of California.								
		<i>Answer</i> km ² [2]								
15	(a)	<i>n</i> is a positive integer. Show that, for all n , $6n^2 + 25n + 11$ is not a prime number.								
		[2]								
	(b)	Hence, determine whether 16261 is a prime number. Show your working clearly.								
	• • • • • •									
	••••	[2]								

16 The diagram represents a plot of land, ABCD. The police is looking for a robber hiding in the land.

Scale: 1 cm represents 1 km



Here are the accounts from three witnesses:

Witness 1: The robber is located more than 6 km away from A.

Witness 2: The robber is located nearer to B than A.

Witness 3: The robber is located nearer to AD than AB.

Shade the region where the robber is hiding.

[4]

17	A = B	{integers $x:1 < x < 21$ } {integers that are perfect squares} {integers that are not prime numbers} {integers that are divisible by 5}	
	(a)	List down all the elements in A , B and	<i>C</i> .
			Answer A =
			<i>B</i> =
			<i>C</i> =[2]
	A nu	umber is chosen randomly from ξ .	
	(b)	Find the number of elements in $B \cap C$	1.
			Answer[1]
	(c)	Hence, find the probability that the cl not divisible by 5.	nosen number is not a prime number and is
			Answer[1]

18	(a)	The prime factorisation of 450 is $2 \times 3^2 \times 5^2$. Express 648 as a product of its prime factors.
		Answer 648 =[1]
	(b)	Using your answer to part (a), determine whether 583200 is a perfect square.

(c) Find the smallest integer n such that 450n is a multiple of 648.

Answer n =[1]

19	(a)	The points $A(0,2)$ and $B(1,0)$ lie on the graph $y = x^2 + ax + b$.
		Find the values of a and b .

Answer $a = \dots$ $b = \dots$ [2]

(b) C is another point on the graph such that the gradient of line AB is twice the gradient of AC. Find the coordinates of point C.

Answer (.....) [3]

20	It is given that	$\overline{AB} =$	(-12)	a > 0	and	$ \overline{BA} = 37$	units
20	it is given that	7110	(a)	,	unu		CILITO.

(a) Find the value of a.

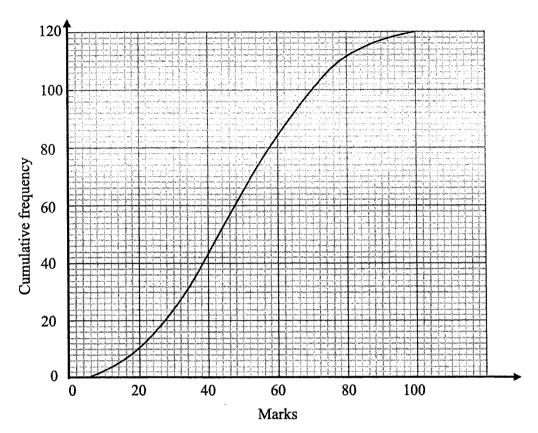
Answer	а	= ,		 					 		 	٠.		.	٦.	2	1
111101101				 ٠.	•	• •	•								· L		J

(b) C is a point (0,10) and $\overrightarrow{AB} = \overrightarrow{DC}$. Find the coordinates of D.

(c) What type of quadrilateral is ABCD? Explain your answer.

.....[1]

The cumulative frequency curve shows the marks obtained by the 120 students in a recent Mathematics Test. The maximum mark is 100.



(a) Complete the grouped frequency table for the marks obtained.

Marks obtained by students, x	Frequency
$0 \le x < 20$	10
$20 \le x < 40$	
$40 \le x < 60$	
$60 \le x < 80$	28
$80 \le x < 100$	8

[1]

(b) Calculate an estimate of the mean mark.

$$0 \le x < 20$$

$$20 \le x < 40$$

$$40 \le x < 60$$

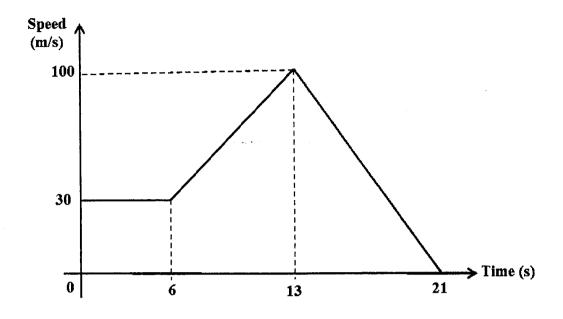
$$60 \le x < 80$$

$$80 \le x < 100$$

Answermarks [1]

(c)	Calculate an estimate of the standard deviation.
	Answermarks [2]
(d)	The passing mark is 50. Two students are chosen at random.
	Find the probability that both of them passed.
	Answer[1]

22 The diagram shows the speed-time graph of a particle.



(a) Find the speed of the particle when t = 12s.

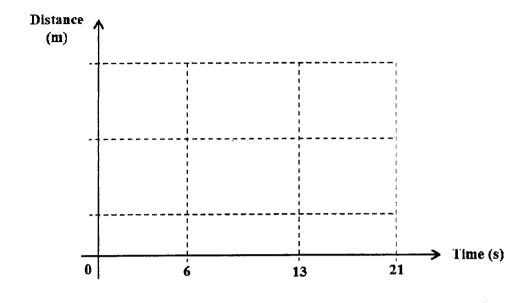
Answer	m/s	[2]	
		r1	

(b) Find the distance covered before the particle starts to slow down.

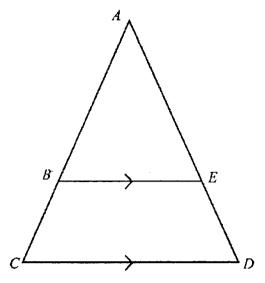
Answer m [2]

(c) Complete the distance-time graph of the particle.

[1]



23



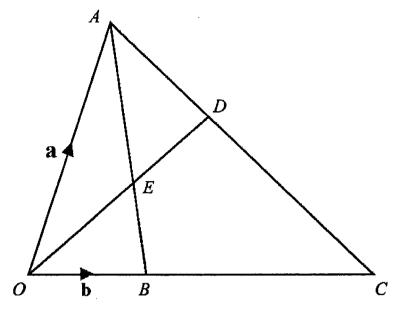
In the diagram, ABC and AED are straight lines and BE is parallel to CD.

(a)	Show that triangle ABE is similar to triangle ACD . Give a reason for each statement you make.
•••••	
	·

(b) Show that
$$\frac{BC}{ED} = \frac{AB}{AE}$$
. [2]

(c)	A circle is drawn with points B , C and D on its circumference. It is full that angle BCD + angle $BED > 180^{\circ}$. Explain why point E is inside	_
•••••		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
		[1]

24



OBC, ADC, AEB and OED are straight lines.

$$\overrightarrow{OA} = \mathbf{a}$$
 and $\overrightarrow{OB} = \mathbf{b}$.

$$OB = \frac{1}{3}OC$$
, $AE : EB = 3:2$ and $OE : ED = 1:1$.

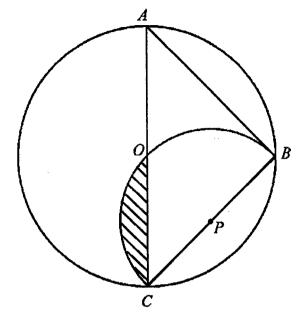
(a) Find \overrightarrow{OE} in terms of a and/or b as simply as possible.

Answer: $\overrightarrow{OE} = \dots [2]$

(b) Find the value of $\frac{\text{area of } \triangle OBE}{\text{area of } BEDC}$.

Answer [2]

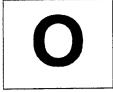
25



AC is a diameter of a circle with centre O. $AC = \sqrt{2}r$ and AB = BC. COB is a semi-circular arc, centre P. What percentage of the circle is **not** shaded?

Answer% [5]

4048/1/GE2/22





JURONG SECONDARY SCHOOL 2022 GRADUATION EXAMINATION 2 SECONDARY 4 EXPRESS/ SECONDARY 5 NORMAL ACADEMIC

CANDIDATE NAME	
CLASS	INDEX NUMBER

MATHEMATICS

4048/02

PAPER 2

24 August 2022 2 hour 30 minutes

Candidates answer on the Question Paper.

READ THESE INSTRUCTIONS FIRST

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At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 100.

For Examiner's Use

This document consists of 26 printed pages including this page.

Mathematical Formulae

Compound interest

Total amount =
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone = πrl

Surface area of a sphere = $4\pi r^2$

Volume of a cone =
$$\frac{1}{3}\pi r^2 h$$

Volume of a sphere =
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Area of triangle
$$ABC = \frac{1}{2}ab\sin C$$

Arc length = $r\theta$, where θ is in radians

Sector area =
$$\frac{1}{2}r^2\theta$$
, where θ is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Statistics

$$Mean = \frac{\sum fx}{\sum f}$$

Standard deviation =
$$\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

Answer all the questions.

- 1 (a) It is given that $y = \frac{5x-2}{3x+1}$.
 - (i) Find y when x = 7.

Answer
$$y = \dots$$
 [1]

(ii) Express x in terms of y.

Answer
$$x = \dots$$
 [2]

(b) Solve $\frac{x-5}{3} - \frac{x+3}{2} = -4$.

Answer
$$x = \dots [2]$$

(c) Solve these simultaneous equations. 3x -

$$3x-2y=10$$

$$2x + y = 23$$

(d) Simplify $\frac{4x^2-9}{6x^2-x-12}$.

Answer [3]

2	Mrs	Teo	is	a	Mathematics	tutor.
4	IVII	100	13	и	Manney	tutor.

She offers tutorial sessions for Lower Secondary and Upper Secondary students on weekdays and on weekends.

Each student attends one session a week for 4 sessions in every month.

The matrix N shows the number of students she tutors every month.

Lower Secondary Upper Secondary

$$\mathbf{N} = \begin{pmatrix} 7 & 6 & \\ 4 & 3 & \end{pmatrix}$$
 Weekday Weekend

(a) Evaluate the matrix M = 4N.

(b) Mrs Teo charges \$70 for each Lower Secondary session and \$80 for each Upper Secondary session.

Represent the session charges in a 2×1 column matrix C.

Answer
$$C = [1]$$

(c) Evaluate the matrix P = MC.

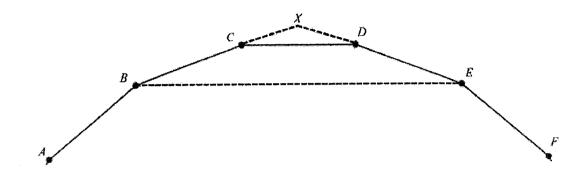
Answer
$$P = [1]$$

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	6	
(d)	State what the elements of P represent.	
	Answer	
		[1]
mon The stud	Teo wants to increase her tuition fees for the weekend sessions by 10% for the last 3 aths before examinations start. number of students registered for the weekday sessions are 10 Lower Secondary ents and 8 Upper Secondary students. On weekends she has 3 Lower Secondary ents and 2 Upper Secondary students.	
(e)	Calculate the total amount of money she earns during this 3 month period.	
•		
	Answer	F4 1

7

3



The diagram below shows part of a regular 18-sided polygon, ABCDEF.... The lines BC and ED are extended to meet at the point X such that XC = XD.

(a) Find $\angle XCD$.

Answer	,,	[1]

(b) Find $\angle CXD$.

(c)	Explain why $BX = EX$.
	Answer

(d) Show that ΔXCD and ΔXBE are similar.

Answer

 4 The first four terms in a sequence of numbers are given below.

$$T_1 = 5^2 - 18 = 7$$

$$T_2 = 6^2 - 22 = 14$$

$$T_3 = 7^2 - 26 = 23$$

$$T_4 = 8^2 - 30 = 34$$

(a) Find T_5 .

Answer	[1]
Answer	 111

(b) Show that the *n*th term of the sequence, T_n , is given by $n^2 + 4n + 2$.

Answer

[2]

(c) Determine and explain if 962 is a term of the sequence.

Answer

[2]

(d)	Find and	simplify	an	expression,	in	terms	of n,	for	T_n	$-T_{n-1}$	۱.
-----	----------	----------	----	-------------	----	-------	-------	-----	-------	------------	----

	Answer	[3]
(e)	Explain why the difference between consecutive terms in the sequence is always odd.	
	Answer	
		Γ17

5 The variables x and y are connected by the equation

$$y = x + \frac{5}{x^2} - 3$$

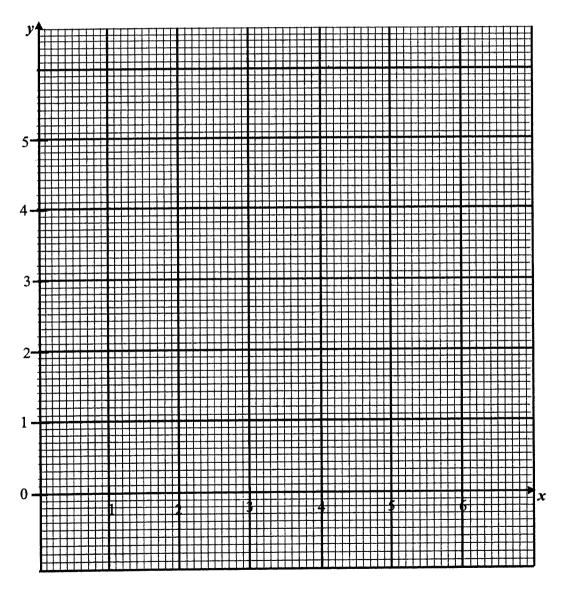
Some corresponding values of x and y are given in the table below.

x	1	1.5	2	2.5	3	4	5	6
у	3	0.7	0.3	0.3	0.0	1.3	p	3.1

(a) Find the value of p.

Answer
$$p = \dots$$
 [1]

(b) On the grid, draw the graph of
$$y = x + \frac{5}{x^2} - 3$$
 for $1 \le x \le 6$.



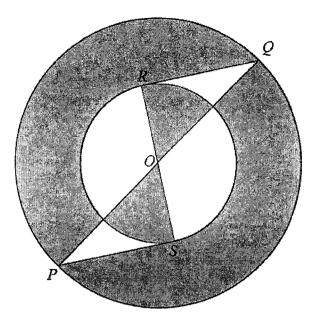
(c)	The equation $x + \frac{5}{x^2} - 3 = 0$ has no solution.						
	Explain how this can be seen from your graph.						
	Answer						
		Γ.					

(d) By drawing a tangent, find the gradient of the curve when x = 1.5.

Answer [2]

(e)	(i)	On the same axes, draw the line with gradient 2 that passes through the point with coordinates $(0.5, 2)$.	[2]
	(ii)	Write down the equation of this line.	
		Answer	[1]
	(iii)	Show, with mathematical justification, that the equation $5-4x^2-x^3=0$ can be solved by finding the points of intersection of the straight line and the curve.	
		Answer	
	(iv)	Use your graphs to solve the equation $5-4x^2-x^3=0$.	[2]
		:	F4.3
		Answer	[1]

6



The diagram shows two concentric circles with centre O. PQ is the diameter of the larger circle and RS is the diameter of the smaller circle. PS and RQ are tangents to the smaller circle.

(a) Show that the triangle *PSO* is congruent to triangle *QRO*. Give a reason for each statement you make.

Answer

(b)	The radius of the larger circle is 8 cm and the radius of the smaller circle is 4.36 cm.										
	(i)	Calculate the area of triangle QRO.									
		Answer cm^2 [3]									
	(ii)	Given that angle QOR is 0.995 radians, calculate the shaded area.									
		Answer cm^2 [4]									

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7 The seating capacity of an auditorium is 300. The seats are categorised as 1, 2, 3 and 4. The costs of the tickets in the categories are in the table below.

CATEGORY	TICKET PRICES
CAT 1	S\$ 348
CAT 2	S\$ 288
CAT 3	S\$ 228
CAT 4	S\$ 148

(a)	The number of seats are distributed in the ratio 1:2:4:5 for CAT 1 to 4 respectively.
	If all the seats are sold out, calculate the ticket sales for category 4.

Answer	\$							•																						[2)	
--------	----	--	--	--	--	--	--	---	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	---	---	---	--

The auditorium has 2 entrances, front entrance F and back entrance B. Entrance F is able to evacuate x people out of the auditorium per second.

(b) (i) Write down an expression, in terms of x, for the time taken in seconds for all 300 people to evacuate if only entrance F is open.

Answer	s	F11
***********		1. * 1

(ii) Entrance F is able to let approximately 2 more people evacuate per second compared to entrance B.

Write down an expression, in terms of x, for the time taken in seconds for all 300 people to evacuate the auditorium if only entrance B is open.

(iii) Usually, only one entrance is open at any time.

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It takes approximately 3 seconds more for all the people to evacuate the
auditorium using entrance B as compared to entrance F .

Form an equation in x and show that it reduces to $x^2 - 2x - 200 = 0$.

Answer

[3]

(iv) Solve the equation $x^2 - 2x - 200 = 0$.

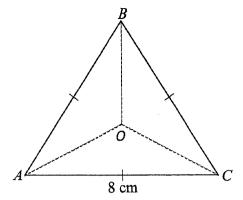
(v) Find the number of people that can be evacuated in 1 minute if only entrance F is opened.

Answer people [2]

8 An equilateral triangle ABC, has sides of 8 cm.

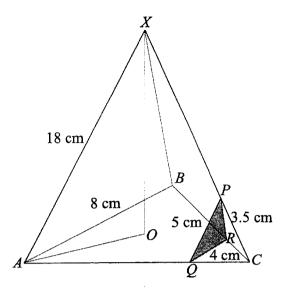
4048/2/GE2/22

O is the centre of the equilateral triangle.



(a) Show that the length of *OA* is 4.619 cm, correct to 3 decimal places. *Answer*

The triangle ABC forms the base of a pyramid. The vertex, X is vertically above O and AX = 18 cm.



(b) Calculate the total surface area of the pyramid.

(c) Part of the pyramid is cut off at triangle PQR such that P is a point on XC, Q is a point on AC and R is a point at BC.
 PQ = 5 cm, QR = 4 cm and PR = 3.5 cm.
 Find angle PQR.

Amornon	0	「つ」
Answer		_ [4]

(d) The ratio of AQ : QC = 3 : 1. Calculate the angle of elevation of X from Q.

Answer° [4]

9 (a) A group of 50 patients had their blood pressure taken.

The results are shown in the table below.

Blood	$100 < x \le 120$	$120 < x \le 140$	$140 < x \le 160$	$160 < x \le 180$
Pressure (mmHg)				
Frequency	27	12	6	5

	Frequency	21	12	0	3	
(i)	State the media	an class of blood	pressure.			
(ii)			or higher indicate who may have hig	es high blood pres		[1]
				Answer	%	[1]
(iii)	Calculate the st	tandard deviation	of the blood pres	sures.		
				Answer	mmHg	[2]
(iv)	The standard d patients was 22		ood pressures tak	en by a second gr	roup of	
	Comment on o information.	ne difference bet	ween the two dist	ributions, making	g reference to this	
	Answer					
					• • • • • • • • • • • • • • • • • • • •	[1]

(b)	A drawer contains 2 blue socks and 6 white socks.
	Two socks are taken from the drawer at random without replacement.
	If the two socks are different colours, then a third sock is taken from the drawer.
	Otherwise, no third sock is taken.

(i) Draw a tree diagram to show the probabilities of the possible outcomes.

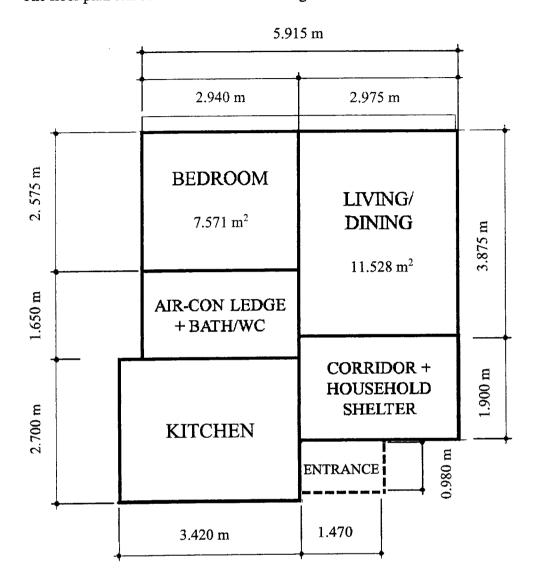
Answer

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Answer [2]

10 Mr Graham bought a 2-room flat in Sembawang.

The floor plan can be modelled as five rectangles as shown below.



(a) Calculate the total floor area of Mr Graham's kitchen.

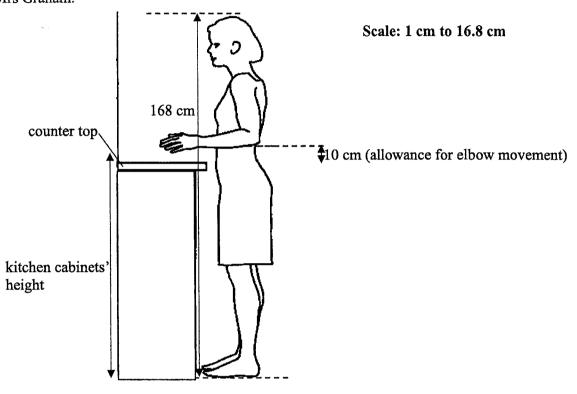
Answer m² [1]

(b) The optimal kitchen cabinets' height, including the counter top, is calculated based on the concept of ergonomics. Ergonomics is the process of designing products that fit the people who use them.

Using the diagram as reference, kitchen cabinet designers view that optimal cabinet height should be the distance between one's elbow and the ground, with 10 cm allowance for elbow movement.

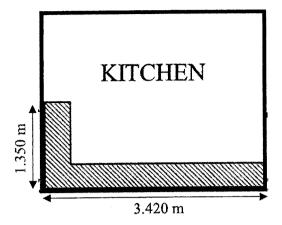
The diagram below shows a drawing of Mrs Graham whose height is 168 cm.

Calculate the range of optimal kitchen cabinets' heights, including the counter top, for Mrs Graham.



Answer	***************************************	cm	2	

(c) Mr Graham plans to install a combination of kitchen cabinets along the L-shaped shaded area in the kitchen.



In the combination, he requires one of the cabinets to have a sink, a corner cabinet and at least one of the other cabinets to have wire basket shelves.

He wants to customise the height of the cabinets to suit Mrs Graham's height. He also wishes to install a counter top for the top of the cabinet, considering to use either granite, ceramic or acrylic as its material.

He has a budget of \$2200 to purchase the kitchen cabinets and L-shaped counter top. Using the information in the tables given on the next page and your answer in (b), propose a possible combination that will best suit Mr Graham's requirements that will optimise storage and space while maximising the use of his budget.

Answer

Table 1: Kitchen Cabinets

Cabinet		2	3	74	5	6
Description	Cabinet with sink, 1 drawer and 1 door (no shelves)	Corner cabinet	Cabinet with 4 drawers	Cabinet with 2 shelves and 2 doors	Cabinet with 1 door and wire basket shelves	Cabinet with 1 drawer, 3 shelves and 1 door.
Cost	\$156	\$166	\$260	\$290	\$166	\$193
Width	50 cm	60 cm	90 cm	80 cm	60 cm	70 cm
Depth	60 cm	60 cm	60 cm	60 cm	60 cm	60 cm

Table 2: Height Customisation for Kitchen Cabinet

Height	Cost per cabinet
50 cm	Free
up to 75 cm	\$15
up to 105 cm	\$25

Table 3: Materials for L-Shaped Counter Top

Materials	Overall Cost		
Granite	\$1200		
Ceramic	\$800		
Acrylic	\$600		

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