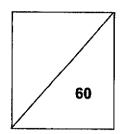


# NORTH VISTA SECONDARY SCHOOL END-OF-YEAR EXAMINATION 2018



NAME:	(	)	CLASS:
SUBJECT: ELEMENTARY MATHEMATICS			DATE: 4 OCTOBER 2018
LEVEL/STREAM: SECONDARY 3 EXPRESS			TIME: 1 HOUR 30 MINUTES
CODE: 4048/01			

#### **READ THESE INSTRUCTIONS FIRST**

Write your name, register number and class on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all questions.

If working is needed for any question, it must be shown with the answer.

Omission of essential working will result in loss of marks.

The use of an approved scientific calculator is expected, where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degree to one decimal place.

For  $\pi$  , use either your calculator value or 3.142, unless the question requires answer in terms of  $\pi$  .

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total of the marks for this paper is 60.

For Exam	iner's Use
Category	Question
Accuracy	
Brackets	
Fractions	
Units	
Others	
Marks Deducted	

This question paper consists of 15 printed pages.

#### Mathematical Formulae

Compound Interest

Total amount = 
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone =  $\pi rl$ 

Surface area of a sphere =  $4\pi r^2$ 

Volume of a cone = 
$$\frac{1}{3}\pi r^2 h$$

Volume of a sphere = 
$$\frac{4}{3}\pi r^3$$

Area of triangle 
$$ABC = \frac{1}{2}ab\sin C$$

Arc length =  $r\theta$ , where  $\theta$  is in radians

Sector area =  $\frac{1}{2}r^2\theta$ , where  $\theta$  is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Statistics

$$Mean = \frac{\sum fx}{\sum f}$$

Standard deviation = 
$$\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

### Answer all the questions.

- 1 The total number of visitors arriving in Singapore in 2008 was  $1.12 \times 10^7$ . The visitors spent a total of 16.5 billion dollars. [1 billion =  $10^9$ ]
  - (a)  $1.12 \times 10^7$  can be written as k million. [1 million =  $10^6$ ] Find k.

(b) What is the average amount of money spent by each visitor? Give your answer correct to the nearest dollar.

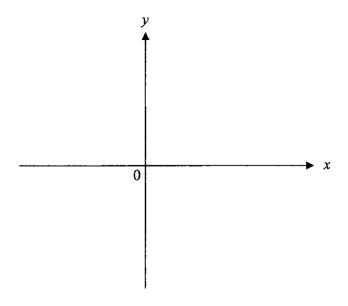
2 Simplify the following

(a) 
$$5x^2y^{-1} \times x^{-3}y$$
,

**(b)** 
$$\left(\frac{16}{x^4}\right)^{-\frac{1}{2}}$$
.

3	(a)	Without the use of calculator, evaluat	$e^{3^0} + 9^{-1} + 3^{-2}.$	
	(b)	Solve $\frac{8^{2x-1}}{4} = \frac{1}{16^x}$ .	Answer	[1]
			Answer	[3]
4		class of 10 girls, their heights are 158 cm, 155 cm, 165 cm, 172 cm, 155 cm		
	For (a)	these heights, find the mode,	Answercm	[1]
	(b)	the mean,		
	(c)	the median.	Answercm	[2]
			Answercm	[1]

5 (a) Sketch the graph of y = -(x-4)(x+2).



[2]

(b) Write down the equation of the line of symmetry of the graph.

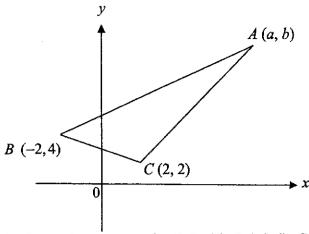
Answer	 [1]	
$\Delta ms we$	 	

(c) Find the coordinates of the turning point.

Answer	(	,	) [1]
--------	---	---	-------

6

6



The figure shows a triangle ABC with B(-2,4), C(2,2) and A(a,b). The gradients of BC, AC and AB are -2n, 2n, n respectively.

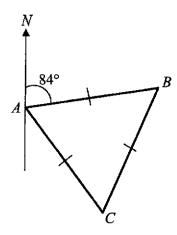
(a) Find (i) the value of n,

Answer	n	==	* # * * * * * * * * * * * * * * * * * *	[1]	l

(ii) the coordinates of A,

6	(a)	(iii) the length of $BC$ .	
		Answer units [	1]
	(b)	Given that the area of triangle $ABC$ is 12 units <sup>2</sup> , find the length of the perpendicular line drawn from $A$ to $BC$ .	
		Answer units [2	2]
			_
7	(a)	Solve the inequality $\frac{2}{3}(x+1) \le x+2 < -(2x-9)$ .	
		Answer	3]
	(b)	Hence, state the largest prime number which satisfies the above inequality.	-
		Answer [	1]
	,		

8



In the diagram above, the points A, B and C form an equilateral triangle and the bearing of B from A is  $084^{\circ}$ .

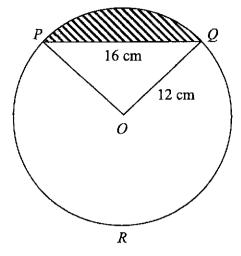
Find the bearing of

(a) C from A,

		Answer°	[1]
<b>(b)</b>	C from B.		

Answer ......° [2]

9 The figure shows a circle with centre O and passes through the points P, Q and R. It has a radius of 12 cm and PQ = 16 cm.

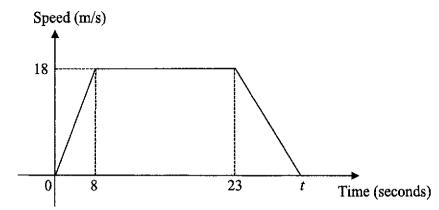


(a)	Show that	at angle $POQ = 1.46$ radians	, correct to 3 significant figures.	
	Answer			
				[1]
<b>(b)</b>	Find the	length of the major arc PRQ		
			Answer cm	[2]

(c) Find the area of the shaded region.

Answer		cm <sup>2</sup> [3	]
--------	--	--------------------	---

10 The diagram below shows the speed-time graph of a moving object.



(a) What is the acceleration of the object at t = 10 seconds?

Answer	m/s <sup>2</sup>	[1]	ĺ
--------	------------------	-----	---

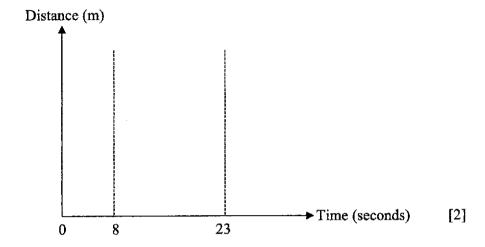
(b) Find the speed of the object when t = 5 seconds.

(c) Find the value of t if the total distance travelled by the object is 450 m.

Answer 
$$t = \dots$$
 [2]

10 (d) On the axes in the answer space below, sketch the distance-time graph for the first 23 seconds and indicate clearly, on the vertical axis, the distance travelled at t = 8 s and t = 23 s.

Answer



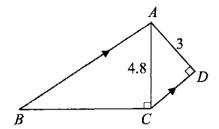
11	Two machines, A and B, are used to manufacture ice cream tubs. 5 ice cream
	tubs manufactured by each machine are randomly selected from each machine.
	The mass of the ice cream tubs manufactured by Machine A are weighed and
	shown in the table below.

					,
Machine A (mass in g)	505	498	502	502	503

(a) Find the mean and standard deviation of the mass of the ice cream tubs manufactured by Machine A.

	Answer Meang	[1]
	Standard Deviationg	[2]
Machine 1	<u>B</u>	
Mean = 50	02 g	
Standard 1	Deviation = 3.16 g	
	· · · · · · · · · · · · · · · · · · ·	
Answer		
	•••••••••••••••••••••••••••••••••••••••	
	•••••••••••••••••••••••••••••••••••••••	
		[1]
	Mean = 5 Standard Based on explain w	Standard Deviationg  Machine B  Mean = 502 g  Standard Deviation = 3.16 g  Based on your answer in (a) and information given above, decide and explain which machine you will recommend to ice cream manufacturers.  Answer

12



The figure is a trapezium, which is made up of two right angled triangles, triangle ABC and triangle ACD. AC = 4.8 cm and AD = 3 cm.

### Calculate

(a) angle ACD,

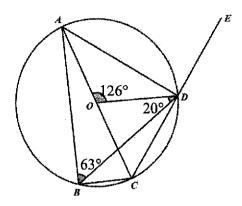
Answer	0	[2]

(b) AB,

(c) area of ABCD.

Answer	,	cm <sup>2</sup>	[2]
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13 In the diagram, A, B, C and D lie on the circumference of the circle. Angle  $AOD = 126^{\circ}$ , angle  $ABD = 63^{\circ}$  and angle  $ODB = 20^{\circ}$ .



(i)	Explain	why	O is	the	centre	of	the	circle	€.
-----	---------	-----	------	-----	--------	----	-----	--------	----

Answer	
	 [1]

- (ii) Find, giving reasons for each answer,
  - (a) angle ACD,

Answer [1
-----------

(b) angle BAD,

************	 ,	 

......[2]

(c) angle BCD.

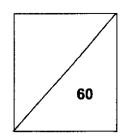
Answer ...... [1]

13	(iii)	Is <i>OD</i> para	allel to BC? Explain your answer.	
		Answer		
				[2]

**End of Paper** 



# NORTH VISTA SECONDARY SCHOOL END-OF-YEAR EXAMINATION 2018



NAME:(	)	CLASS:
SUBJECT: MATHEMATICS (PAPER 2)		DATE: 8 OCTOBER 2018
LEVEL/STREAM: SECONDARY 3 EXPRESS		TIME: 1 HOUR 30 MINUTES
CODE: 4048/2		

#### **READ THESE INSTRUCTIONS FIRST**

Write your name, register number and class on all the work you hand in. Write in dark blue or black pen on both sides of the paper. You may use a pencil for any diagrams or graphs. Do not use staples, paper clips, highlighters, glue or correction fluid.

## Answer all questions.

If working is needed for any question it must be shown with the answer.

Omission of essential working will result in loss of marks.

The use of an approved scientific calculator is expected, where appropriate.

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For  $\pi$ , use either your calculator value or 3.142, unless the question requires the answer in terms of  $\pi$ .

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total of the marks for this paper is 60.

This question paper consists of 6 printed pag	paper consists of a printed pag	yes
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#### Mathematical Formulae

Compound Interest

Total amount = 
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone =  $\pi rl$ 

Surface area of a sphere =  $4\pi r^2$ 

Volume of a cone =  $\frac{1}{3}\pi r^2 h$ 

Volume of a sphere =  $\frac{4}{3}\pi r^3$ 

Area of triangle  $ABC = \frac{1}{2}ab \sin C$ 

Arc length =  $r\theta$ , where  $\theta$  is in radians

Sector area =  $\frac{1}{2}r^2\theta$ , where  $\theta$  is in radians

**Trigonometry** 

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

Statistics

$$Mean = \frac{\sum fx}{\sum f}$$

Standard Deviation = 
$$\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

Answer all the questions.

- 1 (a) Express as a single fraction  $\frac{3x}{(x-3)^2} \frac{7}{2x-6}$ . [3]
  - **(b)** Simplify  $\frac{2s^2 + 9st 5t^2}{3s^2 75t^2} \times \frac{s 5t}{5}$ . [3]
  - (c) It is given that  $\frac{1}{a} + \frac{1}{b} = \frac{1}{c^2}$ .
    - (i) Find b when a = 3, c = -1. [2]
    - (ii) Express c in terms of a and b. [3]
- 2 (a) (i) The cash price of a particular car is \$94000.

Shawn decides to buy this car. He paid a deposit of \$10000 and the rest by monthly instalments of \$1090 over a period of  $7\frac{1}{2}$  years. The bank charges an interest of i % per annum on the amount loaned.

Calculate the value of i. [3]

(ii) Betty buys an identical car which costs the same.

She pays a deposit of one-fifth of the cash price. She then borrows the remaining cost for 3 years at compound interest of 3% per year.

Calculate the total amount of money Betty paid for the car. [4]

(b) The exchange rate between US dollars (\$) and Korean won ( $\Psi$ ) is  $$1 = 1082.50 \Psi$ .

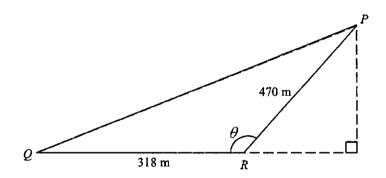
Bill bought 166500₩ from the bank.

Calculate the total amount in US dollars he paid the bank. Leave your answer to the nearest dollar. [2]

[Turn over

BP~407

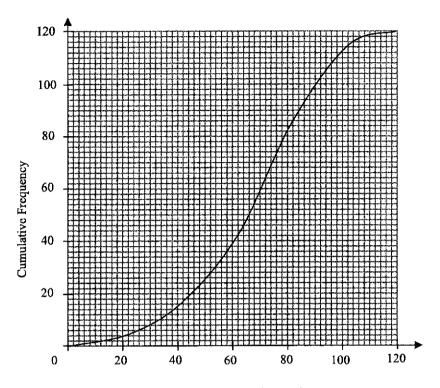
- Ray represented his class in a 10 km race. He started running at a speed of 3 x km/h. After 2 km, he increased his speed by 1 km/h and ran the remaining distance at this speed.
  - Find and simplify, in terms of x, an expression for the time taken by Ray to **(i)** [2] complete the race.
  - Given that Ray's average speed for the whole race was 10.5 km/h, form an [3] (ii) equation in x and show that it reduces to  $10x^2 - 95x - 21 = 0$ .
  - Solve the equation  $10x^2 95x 21 = 0$ . Give your answers correct to 2 (iii) [3] decimal places.
  - Find the time, in hours, Ray would have taken if he had ran the entire race at his initial speed.  $\lceil 1 \rceil$
- 4 The diagram shows three points, P, Q and R on a piece of horizontal land. PR = 470 m and QR = 318 m.



It is given that  $\sin \theta = \frac{7}{25}$  and  $\theta$  is obtuse.

- Calculate the area of  $\Delta PQR$ . [2] (a)
- Without the use of a calculator, show that the value of  $\cos \theta = -\frac{24}{25}$ . (b) [2]
- Hence, find the distance PQ. (c) [3]
- T is the top of a building that is standing vertically at R and the angle of (d) elevation of T from P is 12°. Calculate the height of the building. [2]
- Eli walks along the path PQ until he reaches a point E. Calculate the largest **(e)** angle of depression from T to E. [3]

The graph shows the cumulative frequency curve for the number of hours of community service accumulated over four years by 120 students in Vista Secondary School.



Number of hours of community service

(a) Use your graph to find the

(i) median,

[1]

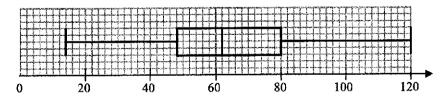
(ii) interquartile range,

[2]

(iii) percentage of students who accumulated more than 100 hours of community service.

[2]

(b) The number of hours of community service accumulated by another 120 students in Venus Secondary School is represented in the following boxand-whisker plot.



Number of hours of community service

Make two comparisons between the number of hours the students spent on community service in the two schools.

[2]

[Turn over

[3]

## 6 Answer the whole of this question on a sheet of graph paper.

An analyst was studying the effect of the introduction of a new policy to a company's business profit. He felt that the amount of profit, y hundred thousand dollars, over a period of x months could be modelled by the equation

$$y = \frac{x^3}{5} + \frac{10}{x} - 10$$
.

Some corresponding values of x and y are given in the following table.

x	0.5	1.5	2	3	4	4.5	5
у	10.03	-2.66	-3.4	-1.27	5.30	10.45	17.00

(a) Using a scale of 2 cm to represent 1 unit, draw a horizontal x-axis for  $0 \le x \le 5$ .

Using a scale of 1 cm to represent 1 unit, draw a vertical y-axis for  $-4 \le y \le 18$ .

On your axes, plot the points given in the table and join them with a smooth curve.

(b) Use your graph to state the period when the company is suffering a loss. [2]

(c) Use your graph to find the solution(s) to the equation  $\frac{x^3}{5} + \frac{10}{x} = 15$  in the range  $0 \le x \le 5$ . [2]

(d) By drawing a tangent, find the gradient of the curve at (1.5, -2.66). [2]

(e) (i) On the same axes, draw the line y = 3x + 1 for  $0 \le x \le 5$ . [1]

(ii) The x-coordinates of the points where the line in (e)(i) intersects the curve are the solutions of the equation  $x^4 - ax^2 - bx + 50 = 0$ . Find the value of a and of b. [2]

#### END OF PAPER

Sec 3E E.Maths EOY P1 2018 Solutions

Qn	Solution	Marks
1a	$1.12 \times 10 \times 10^6$	
	$=11.2\times10^6$	
	k = 11.2	Bi
1b	16.5×10°	
	$1.12 \times 10^7$	
	=\$1473.2142	
	=\$1473	B1
2a	$5x^2y^{-1}\times x^{-3}y$	
	$=5x^{-1}y^0$	
	$=\frac{5}{}$	
	1	B1
2b	$(16)^{-\frac{1}{2}}$	
	$\left( \overline{x^4} \right)$	
	$\left( x^{4}\right) ^{\frac{1}{2}}$	
	$ \left(\frac{16}{x^4}\right)^{-\frac{1}{2}} \\ = \left(\frac{x^4}{16}\right)^{\frac{1}{2}} \\ = \frac{x^2}{4} \\ 3^{-6} + (9)^{-1} + 3^{-2} $	
	$x^2$	
	$=\frac{4}{4}$	B2
3a	$3^{-0} + (9)^{-1} + 3^{-2}$	
	$=1+\frac{1}{9}+\frac{1}{3^2}$	
	1.2	B1
	$=1\frac{1}{9}$	
3b	$=1\frac{2}{9}$ $\frac{8^{2x-1}}{2} = \frac{1}{2}$	
	4 16 <sup>x</sup>	
	$\frac{2^{3(2x-1)}}{2} = \frac{2^0}{4}$	M1
	$\frac{1}{2^2} = \frac{1}{2^{4x}}$	(same base)
	6x - 3 - 2 = 0 - 4x	M1 simplify
	6x - 5 = -4x $10x = 5$	
	1	A1
	$x = \frac{1}{2}$	
4a	155 cm	
4b	Mean 1570	M
	$=\frac{1570}{10}$	M1
	$\begin{vmatrix} 10 \\ =157cm \end{vmatrix}$	A1
	-157cm	

4c	$\frac{155+157}{2} = 156$	B1
5a	2	Shape y-intercept =8 x-intercept = 4, -2
		B2
5b	$\frac{4+(-2)}{2}$	
-	=1	B1
	x=1	D1
5c	(1, 9)	B1
6ai	Gradient of BC $= \frac{4-2}{-2-2}$ $= -\frac{1}{2}$ $-2n = -\frac{1}{2}$ $n = \frac{1}{4}$	B1

6aii	Gradient of $AC = 2n$	
	$\frac{b-2}{a-2} = 2(\frac{1}{4})$	
	2b-4=a-2	
	2b-a=2(1)	M1
	Gradient of $AB = n$	
	$\frac{b-4}{a+2} = \frac{1}{4}$	
-		
	4b-16=a+2	
	4b-18 = a(2)	M1
	Sub (2) into (1)	
	2b - (4b - 18) = 2	
	-2b+18=2	
	b=8	
	a = 4(8) - 18	
	a = 14	A1
	A(14,8)	111
6aiii	Length of BC	
	$=\sqrt{(-2-2)^2+(4-2)^2}$	
	$=\sqrt{20}$	
	= 4.4721	
	= 4.47 <i>units</i>	B1
6b	$\frac{1}{2} \times \sqrt{20} \times h = 12$	M1
	h = 5.3665	A 1
	h = 5.37units	A1
7a	$\frac{2}{3}(x+1) \le x+2 < -(2x-9)$	
	$\frac{2}{3}(x+1) \le x+2$	
	$\left  \frac{2}{3}x + \frac{2}{3} \le x + 2 \right $	
	$-\frac{1}{3}x \le 1\frac{1}{3}$	
	$x \ge -4$	M1
	x+2<-(2x-9)	
	3x < 7	
		M1
	$\frac{x<2\overline{3}}{3}$	
	$\begin{vmatrix} x < 2\frac{1}{3} \\ -4 \le x < 2\frac{1}{3} \end{vmatrix}$	A1

7b	2	B1
8a	Bearing of C from A	
	$=84^{\circ}+60^{\circ}$	
	=144°	B1
8 <b>b</b>	84°-60° = 24°	M1
	Bearing of C from B	
	$=180^{\circ}+24^{\circ}$	
	= 204°	A1
9a	$\sin\theta = \frac{8}{12}$	
	$\theta = 0.72972$	
	$\angle POQ = 0.72972 \times 2$	B1
	=1.45944	
	=1.46rad(shown)	
9b	Reflex angle POQ	
70	$=2\pi-1.45944$	
	=4.82374rad	
	Major arc PRQ	
	$=r\theta$	
	=12(4.82374)	M1
	= 57.88488	1011
	=57.9cm	A1
9c	Area of shaded region	
•		
	$= \frac{1}{2}(12)^2(1.45944) - \frac{1}{2}(12)^2\sin 1.45944$	M2
	=105.07968 - 71.55405	
	=33.52563	
		A1
	$=33.5cm^2$	Ai
	OR	
	$\theta = 1.45944 \times \frac{180^{\circ}}{\pi}$	
	=83.61975	
	$Area = \frac{83.61975}{360} \times \pi (12)^2 - \frac{1}{2} (12)^2 \sin 83.61975$	M2
	=33.5356	
	$=33.5cm^2$	A1
10a	$0 m/s^2$	B1
10b		
<del>-</del>	$\frac{v}{5} = \frac{18}{8}$	
	$v=11\frac{1}{m}/s$	B1

10		3.61
10c	$\frac{1}{2} \times (15+t)(18) = 450$	M1
	15+t=50	A1
	t = 35s	
10d	Answer	
	Distance (m)	Shape - B1
	342 72 0 8 23	Indicate correct distance – B1
		[
11a	$Mean = \frac{2510}{5}$ $= 502g$	B1
	SD for Machine A $= \sqrt{\frac{505^2 + 498^2 + 502^2 + 502^2 + 503^2}{5}} - \left(\frac{2510}{5}\right)^2$ $= \sqrt{\frac{1260046}{5} - \left(\frac{2510}{5}\right)^2}$	Either or M1
	$=\sqrt{\frac{5}{5}-(\frac{5}{5})^2}$	
	= 2.2803	Al
	= 2.28	
11b	I will recommend Machine A as the standard deviation is smaller which	
	means the machine is more consistent in manufacturing the ice-cream tubs.	B1
12a		M1
	$\sin \angle ACD = \frac{3}{4.8}$	
	$\angle ACD = 38.6821$	<b>A</b> 1
	=38.7°	A1
		-t

12b	4.8	
120	$\cos \angle BAC = \frac{4.8}{AB}$	
	4.8	
	$\cos 38.6821 = \frac{4.8}{AB}$	M1
	$AB = \frac{4.8}{\cos 38.6821}$	
	AB = 6.1489	
	AB = 6.15cm	A1
12c	By Pythagoras' Thereom,	
	$CD = \sqrt{4.8^2 - 3^2}$	
	CD = 3.74699	
	Area	
	$= \frac{1}{2} \times (6.1489 + 3.74699) \times 3$	M1
	=14.8437	
	$=14.8cm^2$	A1
13 (i)	Since $\angle AOB = 2 \times \angle ABD$ , O is the centre of circle. ( $\angle$ at centre	
, ,	= 2∠ at circumference)	B1
13(ii)	$\angle ACD = 63^{\circ}$ ( $\angle$ s in same segment)	B1
(a)		
13(ii) (b)	$\angle ODA = \frac{180 - 126}{2} = 27^{\circ}$ (base $\angle$ s of isos. $\triangle$ )	M1
	$\angle BAD = 180 - 63 - 20 - 27 = 70^{\circ} \text{ (sum of } \angle \text{s in } \Delta\text{)}$	A1
13	$\angle BCD = 180 - 70 = 110^{\circ}$ ( $\angle$ s in opp. segment)	B1
(ii)		
(c)		3.51
13	$\angle DBC = 27^{\circ} (\angle s \text{ in same segment})$	M1 A1
(iii)	Since $\angle ODB \neq \angle DBC$ , OD is not parallel to BC.	AI
{		

## 3E EM P2 Marking Scheme

Question	Marking Scheme	Marks
1 (a)	3 <i>x</i> 7	M1
	$\frac{3x}{(x-3)^2} - \frac{7}{2(x-3)}$	
	6x-7(x-3)	М1
	$=\frac{6x-7(x-3)}{2(x-3)^2}$	
	1	Al
	$=\frac{-x+21}{2(x-3)^2}$	AI
1 (b)	$\frac{2s^2 + 9st - 5t^2}{3s^2 - 75t^2} \times \frac{s - 5t}{5}$	M2
	$\frac{-3s^2-75t^2}{5}$	(cross method
		and diff
	$= \frac{(2s-t)(s+5t)}{3(s-5t)(s+5t)} \times \frac{s-5t}{5}$	of
	$=\frac{2s-t}{15}$	squares)
	= 15	
		A1
1 (c) (i)	$\frac{1}{3} + \frac{1}{b} = \frac{1}{1}$	M1
	$\begin{bmatrix} 3 & b \end{bmatrix}$	
	$\frac{1}{b} = \frac{2}{3}$	, ,
	$b = 1\frac{1}{2}$ $\frac{1}{a} + \frac{1}{b} = \frac{1}{c^2}$	A1
1 (c) (ii)		711
()()	$\frac{a}{a} + \frac{b}{b} = \frac{a}{c^2}$	
	b+a 1	M1
	$\frac{b+a}{ab} = \frac{1}{c^2}$	141.1
	$c^2 = \frac{ab}{b+a}$	
	$c - \frac{b+a}{b+a}$	
	$c = \pm \sqrt{\frac{ab}{b+a}}$	A2 (A1
	$b-1\sqrt{b+a}$	for ±)
2 (a) (i)	Interest = $1090 \times 7.5 \times 12 + 10000 - 94000 = $14100$	M1
	$14100 = \frac{84000 \times i \times 7.5}{100}$	M1
	100	1411
	$i = 2\frac{5}{21}\%$	
	<u>Z1</u>	A1

2 (a) (ii)	Amount borrowed = $\frac{4}{5} \times 94000 = $75200$	
	9	
	Amount owed = $75200(1 + \frac{3}{100})^3 = $82173.0704$	M1
	Amount Betty paid = $82173.0704 + \frac{1}{5} \times 94000$	M1
	=\$100973.07(2 $dp$ )	Al
2 (b)	Total amount = $\frac{101.5}{100} \times 166500 \div 1082.50$	M1
	=\$153.81	
	=\$154	A1
3 (i)	$Time = \frac{2}{x} + \frac{8}{x+1}$	M1
	$=\frac{2x+2+8x}{x(x+1)}$	
	$-\frac{10x+2}{h}$	
	$=\frac{10x+2}{x(x+1)}h$	A1
3 (ii)	$\frac{10}{10x+2} = 10.5$	M1
	$\overline{x(x+1)}$	
	$\frac{10x(x+1)}{10x+2} = 10.5$	M1
		M1
	$10x^2 + 10x = 105x + 21$	1411
3 (iii)	$10x^2 - 95x - 21 = 0$	M1
J (III)	$x = \frac{95 \pm \sqrt{(-95)^2 - 4(10)(-21)}}{2(10)}$	
	2(10)	M1
	$=\frac{95\pm\sqrt{9865}}{20}$	<b>M</b> 1
	= 9.7161  or  -0.2161	
	= 9.72  or  -0.22	A1
3 (iv)		B1
	$\frac{10}{9.7161} = 1.03h$	
4 (a)	Area = $\frac{1}{2}(318)(470)(\frac{7}{25})$	M1
	$=20924\frac{2}{5}m^2$	A1

$\sin\theta = \frac{1}{2.5}$ $\sin x = \frac{7}{2.5}, \text{ where x is acute}$ By Pythagoras' Theorem, $adj = \sqrt{25^2 - 7^2} = 24$ $\cos x = \frac{24}{2.5}$ $\cos\theta = -\frac{24}{2.5}$ $4 \text{ (c)}$ $PQ^2 = 318^2 + 470^2 - 2(318)(470)(-\frac{24}{2.5})$ $= 780.3763$ $= 780m(3sf)$ A1 $4 \text{ (d)}$ $\tan 12^\circ = \frac{TR}{470}$ $TR = 470 \tan 12^\circ$ $= 99.9015$ $= 99.9015$ $= 99.90(3sf)$ A1 $4 \text{ (e)}$ Let the perpendicular dist be h. $\frac{1}{2}(h)(780.3763) = 20924\frac{2}{5}$ $h = 53.6264$ $= 53.6m(3sf)$ Let the angle of depression be x. $\tan x = \frac{99.9015}{99.9015}$ $\tan x = \frac{99.9015}{5(a)(ii)}$ $10 \text{ hours}$ $5 \text{ (a) (ii)}$ $10 \text{ Q3}=84$ $Q1=54$ $QR$ $= 84 - 54$ $= 30 hours$ $10 \text{ M1}$ $120 - 112$ $120 - 112$ $120 - 112$ $120 - 1212$ $120 \times 100\%$ $= 6\frac{2}{3}\%$ A1			
By Pythagoras' Theorem, $adj = \sqrt{25^2 - 7^2} = 24$ $cos x = \frac{24}{25}$ $cos \theta = -\frac{24}{25}$ A1  4 (c) $PQ^2 = 318^2 + 470^2 - 2(318)(470)(-\frac{24}{25})$ $= 780.3763$ $= 780m(3sf)$ A1  4 (d) $tan 12^\circ = \frac{TR}{470}$ $TR = 470 tan 12^\circ$ $= 99.9015$ $= 99.9m(3sf)$ A1  4 (e) $Let the perpendicular dist be h.$ $\frac{1}{2}(h)(780.3763) = 20924\frac{2}{5}$ $h = 53.6264$ $= 53.6764$ $= 53.6764$ $= 53.6764$ $= 53.6764$ $= 53.6764$ $= 61.7734$ $= 61.8^\circ(1dp)$ A1  5 (a) (ii) $Q3 = 84$ $Q1 = 54$ $IQR$ $= 84 - 54$ $= 30hours$ 5 (a) (iii) $\frac{Q3 = 84}{120}$ $\frac{Q1 = 84}{$	4 (b)	$\sin\theta = \frac{7}{25}$	
By Pythagoras' Theorem, $adj = \sqrt{25^2 - 7^2} = 24$ $cos x = \frac{24}{25}$ $cos \theta = -\frac{24}{25}$ A1  4 (c) $PQ^2 = 318^2 + 470^2 - 2(318)(470)(-\frac{24}{25})$ $= 780.3763$ $= 780m(3sf)$ A1  4 (d) $tan 12^\circ = \frac{TR}{470}$ $TR = 470 tan 12^\circ$ $= 99.9015$ $= 99.9m(3sf)$ A1  4 (e) $Let the perpendicular dist be h.$ $\frac{1}{2}(h)(780.3763) = 20924\frac{2}{5}$ $h = 53.6264$ $= 53.6764$ $= 53.6764$ $= 53.6764$ $= 53.6764$ $= 53.6764$ $= 61.7734$ $= 61.8^\circ(1dp)$ A1  5 (a) (ii) $Q3 = 84$ $Q1 = 54$ $IQR$ $= 84 - 54$ $= 30hours$ 5 (a) (iii) $\frac{Q3 = 84}{120}$ $\frac{Q1 = 84}{$		$\sin x = \frac{7}{25}$ , where x is acute	
$a0 = \sqrt{25} - V = 24$ $\cos x = \frac{24}{25}$ $\cos \theta = -\frac{24}{25}$ $1 + \sqrt{25}$ $2 + \sqrt$		1 23	
$cos \theta = -\frac{24}{25}$ $4 (c)$ $PQ^{2} = 318^{2} + 470^{2} - 2(318)(470)(-\frac{24}{25})$ $= 780.3763$ $= 780m(3sf)$ $4 (d)$ $tan 12^{\circ} = \frac{TR}{470}$ $TR = 470 tan 12^{\circ}$ $= 99.9015$ $= 99.9m(3sf)$ $4 (e)$ $Let the perpendicular dist be h. \frac{1}{2}(h)(780.3763) = 20924\frac{2}{5} h = 53.6264 = 53.6m(3sf) Let the angle of depression be x. tan x = \frac{99.9015}{53.6264} x = 61.7734 = 61.8^{\circ}(1dp) 5 (a) (ii) Q3=84 Q1=54 QR = 84-54 = 30hours 5 (a) (iii) \frac{120-112}{120} \times 100\% = 6\frac{2}{3}\% A1  M2  M3  M1  A1  M1  A1  A1  A1  A1  A1  A1  A1$		$adj = \sqrt{25^2 - 7^2} = 24$	M1
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		$\cos x = \frac{24}{25}$	
$PQ = \sqrt{318^2 + 470^2 - 2(318)(470)(-\frac{24}{25})}$ $= 780.3763$ $= 780m(3sf)$ A1 $4 \text{ (d)} \qquad \tan 12^\circ = \frac{TR}{470}$ $TR = 470 \tan 12^\circ$ $= 99.9015$ $= 99.9m(3sf)$ A1 $4 \text{ (e)} \qquad \text{Let the perpendicular dist be h.}$ $\frac{1}{2}(h)(780.3763) = 20924\frac{2}{5}$ $h = 53.6264$ $= 53.6m(3sf)$ $\text{Let the angle of depression be x.}$ $\tan x = \frac{99.9015}{53.6264}$ $x = 61.7734$ $= 61.8^\circ(1dp)$ A1 $5 \text{ (a) (ii)} \qquad 70 \text{ hours}$ $5 \text{ (a) (iii)} \qquad Q3=84$ $Q1=54$ $IQR$ $= 84-54$ $= 30hours$ $= 30hours$ $11$ $120-112$ $120$ $120$ $= 6\frac{2}{3}\%$ A1		$\cos\theta = -\frac{24}{25}$	<b>A</b> 1
$= 780.3763 = 780m(3sf)$ $= 100 \text{ an } 12^{\circ} = \frac{TR}{470}$ $= 99.9015 = 99.9m(3sf)$ $= 99.9m(3sf)$ $= 100 \text{ Al } 100  Al$	4 (c)	$PQ^2 = 318^2 + 470^2 - 2(318)(470)(-\frac{24}{25})$	M2
$ = 780m(3sf) $ $4 (d) $ $ \tan 12^{\circ} = \frac{TR}{470} $ $ TR = 470 \tan 12^{\circ} $ $ = 99.9015 $ $ = 99.9m(3sf) $ $4 (e) $		$PQ = \sqrt{318^2 + 470^2 - 2(318)(470)(-\frac{24}{25})}$	
$4 \text{ (d)} \qquad \tan 12^{\circ} = \frac{TR}{470}$ $TR = 470 \tan 12^{\circ}$ $= 99.9015$ $= 99.9m(3sf)$ $4 \text{ (e)} \qquad \text{Let the perpendicular dist be h.}$ $\frac{1}{2}(h)(780.3763) = 20924\frac{2}{5}$ $h = 53.6264$ $= 53.6m(3sf)$ $\text{Let the angle of depression be x.}$ $\tan x = \frac{99.9015}{53.6264}$ $x = 61.7734$ $= 61.8^{\circ}(1dp)$ $5 \text{ (a) (ii)} \qquad Q3=84$ $Q1=54$ $IQR$ $= 84-54$ $= 30hours$ $5 \text{ (a) (iii)} \qquad \frac{120-112}{120} \times 100\%$ $= 6\frac{2}{3}\%$ $\text{M1}$		= 780.3763	
		=780m(3sf)	A1
$TR = 470 \tan 12^{\circ}$ $= 99.9015$ $= 99.9m(3sf)$ A1  4 (e) Let the perpendicular dist be h. $\frac{1}{2}(h)(780.3763) = 20924\frac{2}{5}$ $h = 53.6264$ $= 53.6m(3sf)$ Let the angle of depression be x. $\tan x = \frac{99.9015}{53.6264}$ $x = 61.7734$ $= 61.8^{\circ}(1dp)$ A1  5 (a) (i) 70 hours B1  5 (a) (ii) Q3=84 Q1=54 IQR $= 84-54$ $= 30hours$ A1  5 (a) (iii) $\frac{120-112}{120} \times 100\%$ $= 6\frac{2}{3}\%$ A1	4 (d)	$\tan 12^\circ = \frac{TR}{470}$	M1
$= 99.9m(3sf)$ 4 (e) Let the perpendicular dist be h. $\frac{1}{2}(h)(780.3763) = 20924\frac{2}{5}$ M1 $h = 53.6264$ $= 53.6m(3sf)$ Let the angle of depression be x. $\tan x = \frac{99.9015}{53.6264}$ M1 $x = 61.7734$ $= 61.8^{\circ}(1dp)$ A1 $5 (a) (ii)$ Q3=84 Q1=54 IQR $= 84 - 54$ $= 30hours$ A1 $5 (a) (iii)$ $\frac{120 - 112}{120} \times 100\%$ $= 6\frac{2}{3}\%$ A1			
4 (e) Let the perpendicular dist be h. $\frac{1}{2}(h)(780.3763) = 20924\frac{2}{5}$ M1 $h = 53.6264$ $= 53.6m(3sf)$ Let the angle of depression be x. $\tan x = \frac{99.9015}{53.6264}$ M1 $x = 61.7734$ $= 61.8^{\circ}(1dp)$ A1 $5 \text{ (a) (ii)}  Q3=84$ $Q1=54$ $IQR$ $= 84-54$ $= 30hours$ A1 $5 \text{ (a) (iii)}  \frac{120-112}{120} \times 100\%$ M1 $= 6\frac{2}{3}\%$		=99.9015	
$ \frac{1}{2}(h)(780.3763) = 20924 \frac{2}{5} $ $ h = 53.6264 $ $ = 53.6m(3sf) $ Let the angle of depression be x. $ \tan x = \frac{99.9015}{53.6264} $ $ x = 61.7734 $ $ = 61.8°(1dp) $ A1 $ \frac{5 \text{ (a) (ii)}}{5 \text{ (a) (iii)}} $ $ \frac{23=84}{1QR} $ $ = 84-54 $ $ = 30hours $ A1 $ \frac{120-112}{120} \times 100\% $ $ = 6\frac{2}{3}\% $ A1		=99.9m(3sf)	A1
$h = 53.6264$ $= 53.6m(3sf)$ Let the angle of depression be x. $\tan x = \frac{99.9015}{53.6264}$ $x = 61.7734$ $= 61.8^{\circ}(1dp)$ A1 $5 \text{ (a) (ii)}$ $Q3=84$ $Q1=54$ $IQR$ $= 84-54$ $= 30hours$ $5 \text{ (a) (iii)}$ $\frac{120-112}{120} \times 100\%$ $= 6\frac{2}{3}\%$ A1  M1  A1  A1	4 (e)	Let the perpendicular dist be h.	
$= 53.6m(3sf)$ Let the angle of depression be x. $\tan x = \frac{99.9015}{53.6264}$ $x = 61.7734$ $= 61.8^{\circ}(1dp)$ A1 $5 \text{ (a) (ii)}  Q3=84$ $Q1=54$ $IQR$ $= 84-54$ $= 30hours$ $5 \text{ (a) (iii)}  \frac{120-112}{120} \times 100\%$ $= 6\frac{2}{3}\%$ M1 $A1$		$\frac{1}{2}(h)(780.3763) = 20924\frac{2}{5}$	M1
Let the angle of depression be x. $ \tan x = \frac{99.9015}{53.6264} $ $x = 61.7734$ $= 61.8^{\circ}(1dp)$ A1  S (a) (i) 70 hours S (a) (ii) Q3=84 Q1=54 IQR $= 84-54$ $= 30hours$ A1  S (a) (iii) $\frac{120-112}{120} \times 100\%$ $= 6\frac{2}{3}\%$ A1		h = 53.6264	
$\tan x = \frac{99.9015}{53.6264}$ $x = 61.7734$ $= 61.8^{\circ}(1dp)$ A1 $5 \text{ (a) (ii)}$ $Q3=84$ $Q1=54$ $IQR$ $= 84-54$ $= 30hours$ $5 \text{ (a) (iii)}$ $\frac{120-112}{120} \times 100\%$ $= 6\frac{2}{3}\%$ M1  A1		=53.6m(3sf)	
		Let the angle of depression be x.	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		99.9015	N/1
		$\tan x = \frac{1}{53.6264}$	1411
5 (a) (i) 70 hours B1  5 (a) (ii) Q3=84 Q1=54 IQR = 84-54 = 30 hours  5 (a) (iii) $\frac{120-112}{120} \times 100\%$ $= 6\frac{2}{3}\%$ A1  B1  A1		x = 61.7734	
5 (a) (ii) Q3=84 Q1=54 IQR = 84-54 = 30hours A1  5 (a) (iii) $\frac{120-112}{120} \times 100\%$ $= 6\frac{2}{3}\%$ A1			A1
Q1=54 IQR = 84-54 = 30hours  M1 A1 $\frac{120-112}{120} \times 100\%$ $\frac{6^2}{3}\%$ A1			B1
IQR = 84-54 = 30hours A1 $5 \text{ (a) (iii)}$ $\frac{120-112}{120} \times 100\%$ M1 = $6\frac{2}{3}\%$ A1	5 (a) (11)	1 *	
5 (a) (iii) $\frac{120 - 112}{120} \times 100\%$ $= 6\frac{2}{3}\%$ A1		I =	
$ \frac{120}{120} \times 100\% \\ = 6\frac{2}{3}\% $ A1		= 30hours	A1
$= 6\frac{2}{3}\%$ 5 (b) IQR for Venus Sec	5 (a) (iii)	120 ×100%	M1
5 (b) IQR for Venus Sec		$=6\frac{2}{3}\%$	A1
	5 (b)	IQR for Venus Sec	

	00 40	1
	= 80 - 48 $= 32$	
	= 32	
	1. Students from Vista Sec School spend more time on	
	community service as the median hours is higher.  2. Students from Venus Sec School community service hours	
	is more varied as the interquartile range is larger.	B2
6 (a), (e) (i)	y	P2 C1
.,		
		Bl
6 (b)	$0.75 months < t < 3.25 months (\pm 0.5)$	B2
6 (c)	$\frac{x^3}{5} + \frac{10}{x} = 15$	
	$\frac{x^3}{5} + \frac{10}{x} - 10 = 15 - 10 = 5$	
	$ \begin{vmatrix} 5 & x \\ y = 5 \end{vmatrix} $	M <sub>1</sub>
	$x = 0.45 \text{ or } 4 (\pm 0.5)$	A1
6 (d)	1.6+5	M1
· (-)	$m = \frac{1}{-0.7 - 2.6}$	(drawin
	$=-2\ (\pm 0.5)$	g of tangent)
		A1
		! !
6 (e) (ii)	y = 3x + 1	
6 (e) (ii)		
6 (e) (ii)	$y = \frac{x^3}{5} + \frac{10}{x} - 10$	
6 (e) (ii)	$y = \frac{x^3}{5} + \frac{10}{x} - 10$ $3x + 1 = \frac{x^3}{5} + \frac{10}{x} - 10$	
6 (e) (ii)	$y = \frac{x^3}{5} + \frac{10}{x} - 10$	
6 (e) (ii)	$y = \frac{x^3}{5} + \frac{10}{x} - 10$ $3x + 1 = \frac{x^3}{5} + \frac{10}{x} - 10$	
6 (e) (ii)	$y = \frac{x^3}{5} + \frac{10}{x} - 10$ $3x + 1 = \frac{x^3}{5} + \frac{10}{x} - 10$ $15x^2 + 5x = x^4 + 50 - 50x$	B1